

## Exercises – Week 8

### Trees

1. Write a function that takes a binary tree and returns the list of nodes that have a single child. The order of the nodes in the list will be that of the inorder traversal.
2. Write a function that takes a binary tree and returns the total number of nodes in the tree.
3. **Traversal of arbitrary trees:** Modify traversal functions to work on arbitrary trees (each node has a list of children). Use list traversal functions. For inorder, first traverse the head of the list, then the root and then tail of the list.
4. **Indented Printing:** Write a function that displays a binary tree of integers in preorder, one node per line, preceding the value of the node by a number of spaces equal to twice its depth (two spaces for each level).
5. **Removing a node:** Write a function that takes a value and a binary search tree as parameters and returns the tree from which the value was removed (if present).

Tips:

- if the tree is not empty:
  - if the given value is identical to the root key then we have found the searched node. We proceed as follows:
    - if the node is terminal (the left subtree and the right subtree are empty) this node will be deleted, and the address retained by the parent in its place becomes None;
    - if only the left subtree is non-empty the node will be deleted, and the address retained by the parent in its place becomes the address of the left subtree;
    - if only the right subtree is non-empty the node will be deleted, and the address retained by the parent in its place becomes the address of the right subtree;
    - if both subtrees are not empty:
      - the biggest node in the left subtree is identified (the rightmost node of the left subtree). This node cannot have a right subtree!
      - the information from this node is copied into our searched node;
      - the identified node is deleted. The deletion is performed as if the node is terminal or as if the node has only left subtrees;
  - if the given value is smaller than the root key, the search continues in the left subtree;

- if the given value is greater than the root key, the search continues in the right subtree;
- if the tree is empty:
  - the searched value does not exist in the tree.